

Challenges for Efficient Query Evaluation on Structured Probabilistic Data



SUM2016

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A probabilistic database

Amarillii Antoine, Maniu Silviu, Monet Mikael

| S | |
|---|---|
| d | e |
| f | c |
| a | e |
| c | e |

| R | |
|---|---|
| a | d |
| f | e |
| d | a |
| b | e |

| Q | | |
|---|---|---|
| c | e | f |

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| R | | |
|---|---|------|
| a | d | 0.2 |
| f | e | 0.7 |
| d | a | 0.13 |
| b | e | 0.81 |

| S | | |
|---|---|-------|
| d | e | 0.005 |
| f | c | 0.9 |
| a | e | 0.7 |
| c | e | 0.23 |

| Q | | |
|---|---|---|
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| c | e | f | 0.66 |

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TID model

Probability of a possible world

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A possible
World I



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Probability $\text{Pr}(I)$ of this possible world =
 $0.7 * 0.13 * 0.23 * 0.66$

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 $0.7 * 0.13 * 0.23 * 0.66$
 $* (1 - 0.2) * (1 - 0.81) * (1 - 0.005) * (1 - 0.9) * (1 - 0.7).$

Probabilistic query evaluation (PQE)

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- ▶ Focus on Boolean queries (yes/no)

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- ▶ Probability of a query Q on probabilistic instance \mathfrak{T} :

$$P(Q) = \sum_{I \subseteq \mathfrak{T}, Q \models I} \Pr(I)$$

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- ▶ Focus on Boolean queries (yes/no)
- ▶ Probability of a query Q on probabilistic instance \mathfrak{T} :

$$P(Q) = \sum_{I \subseteq \mathfrak{T}, Q \models I} \Pr(I)$$

- ▶ Problem: in general #P-hard

1) Approximate probability computation

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- ▶ Monte-Carlo sampling
- ▶ Inconvenient: running time quadratic in desired precision.
⇒ Not adequate for low probabilities.

2) Restricting the class of queries

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- ▶ Simple conjunctive query $\exists x,y \ R(x),T(x,y),S(y)$ is already #P-hard !

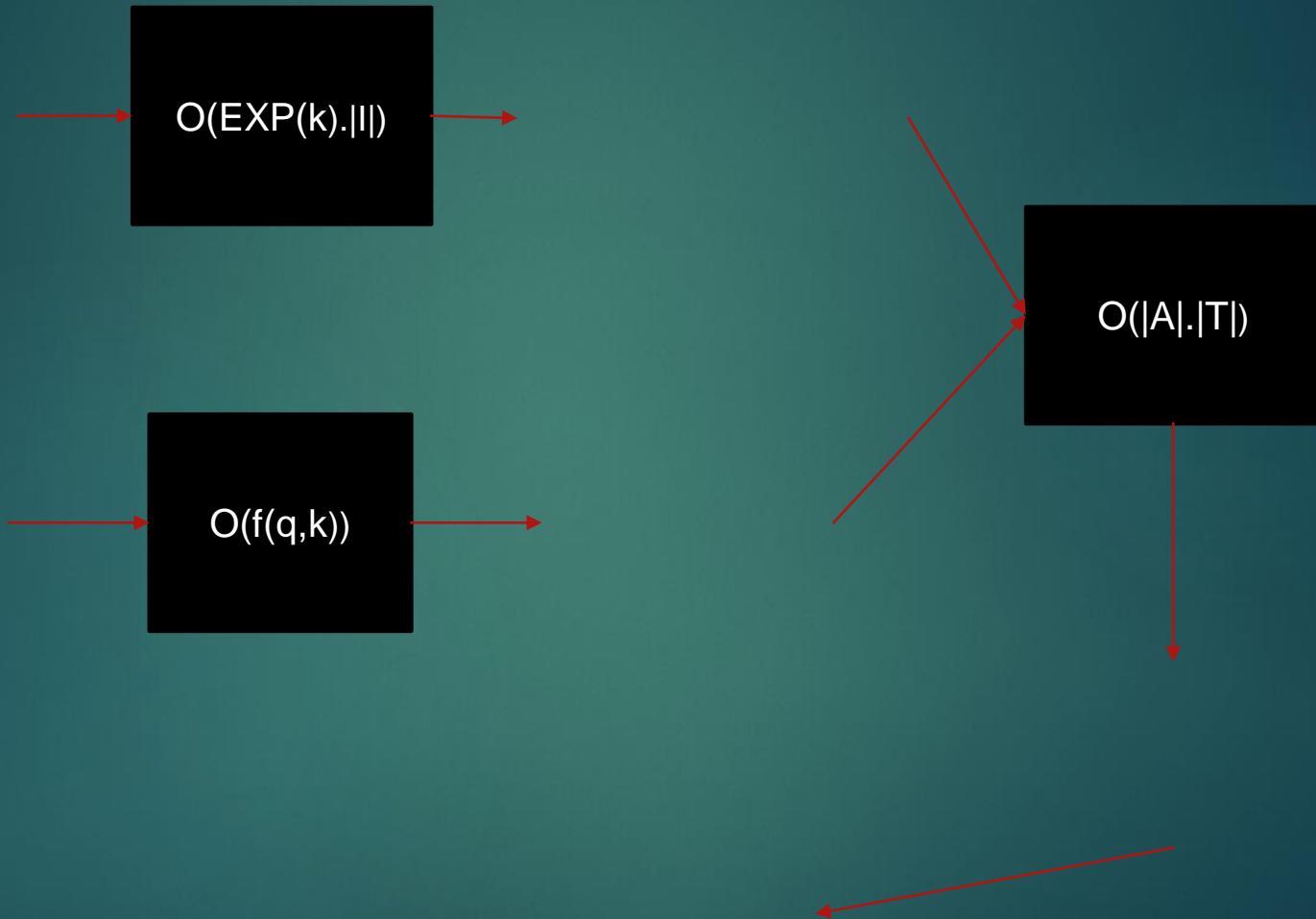
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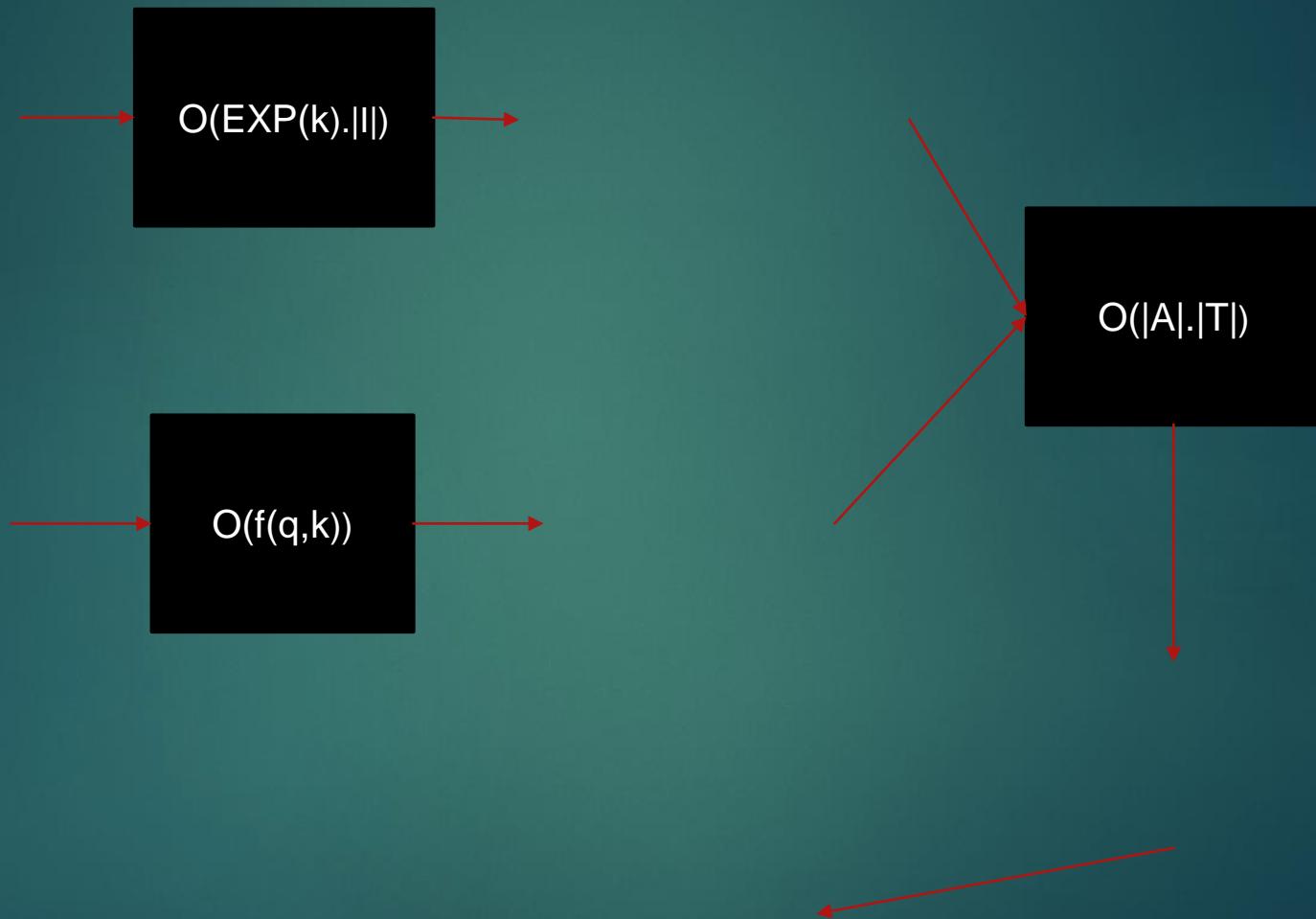
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- ▶ Simple conjunctive query $\exists x,y \ R(x),T(x,y),S(y)$ is already #P-hard !
- ▶ Criterion is to crisp

3) Restricting the shape of the instances

- ▶ Bound the *treewidth* of instances by a constant.
- ▶ Treewidth: measure used to tell how far a graph is from being a tree



Instance I
of treewidth
 k



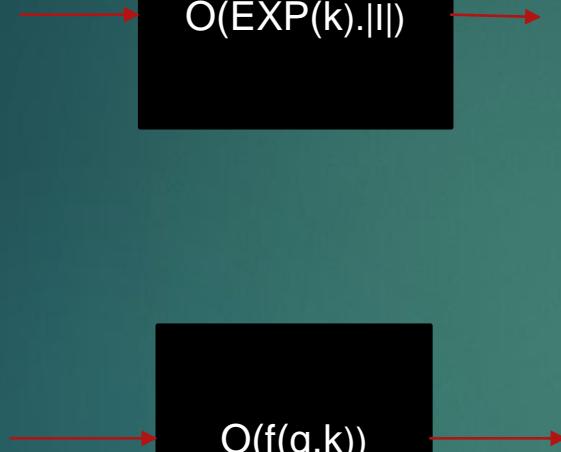
Instance I
of treewidth
k

$$O(\text{EXP}(k).|I|)$$

Tree
decomposition
 T

$$O(|A|.|T|)$$

$$O(f(q,k))$$



Instance I
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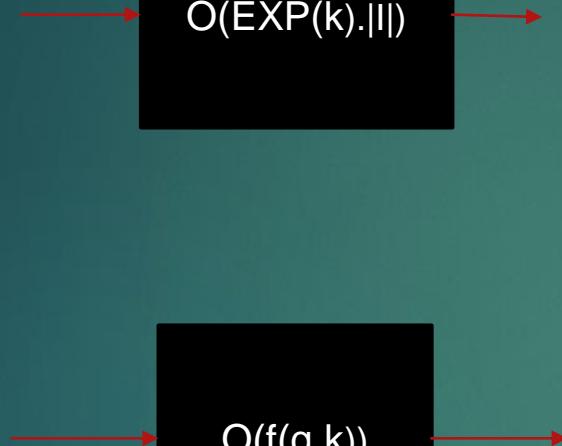
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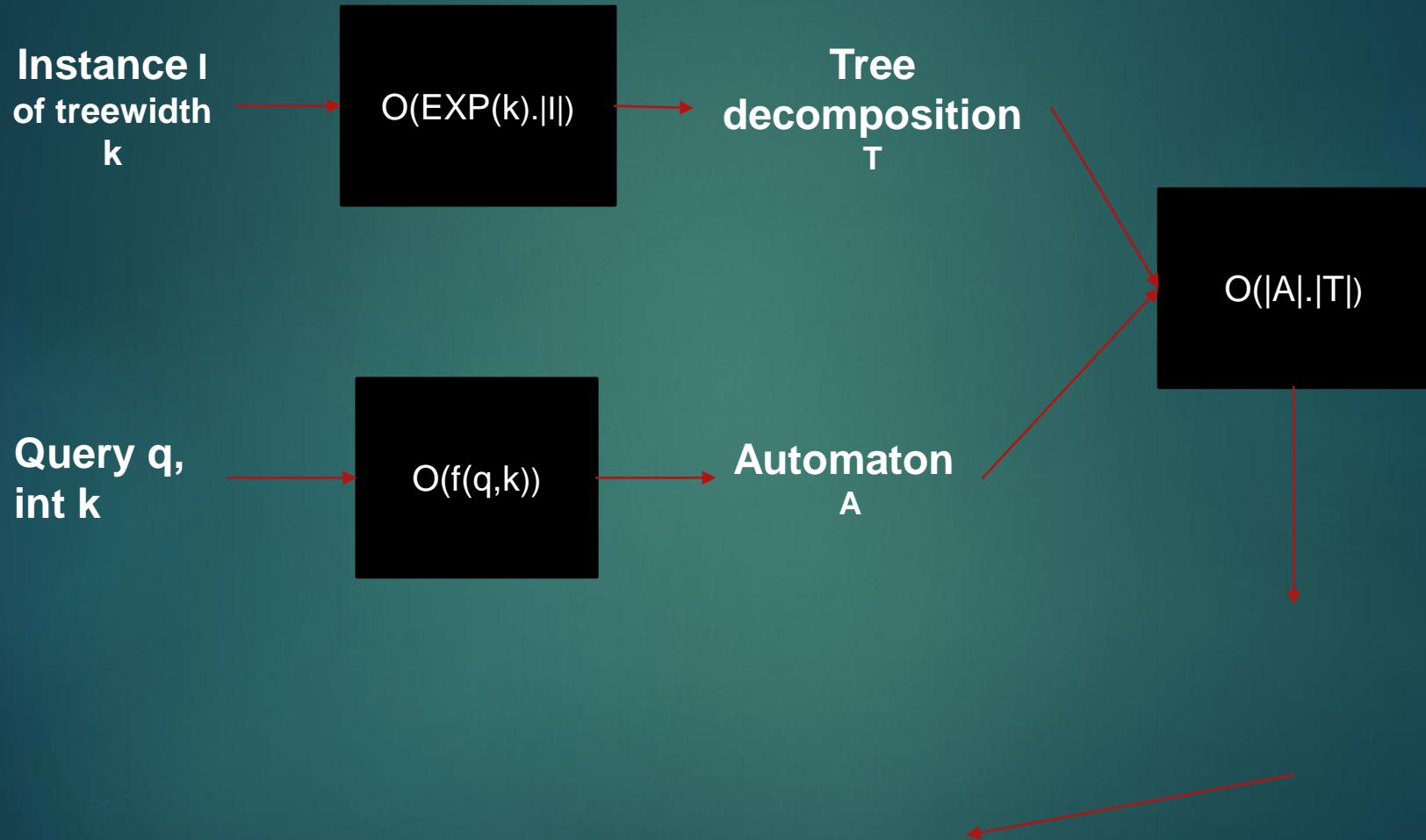
Tree
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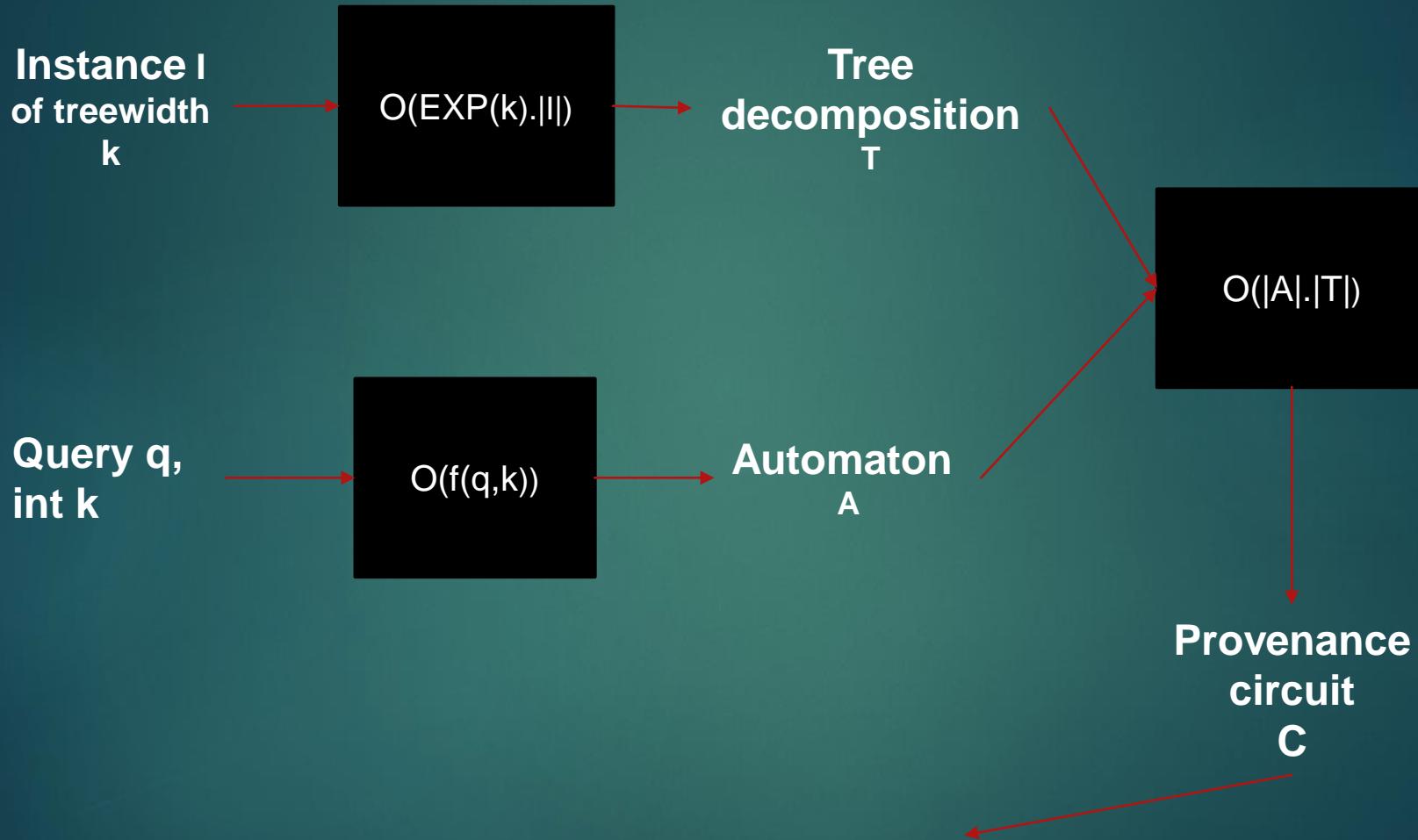
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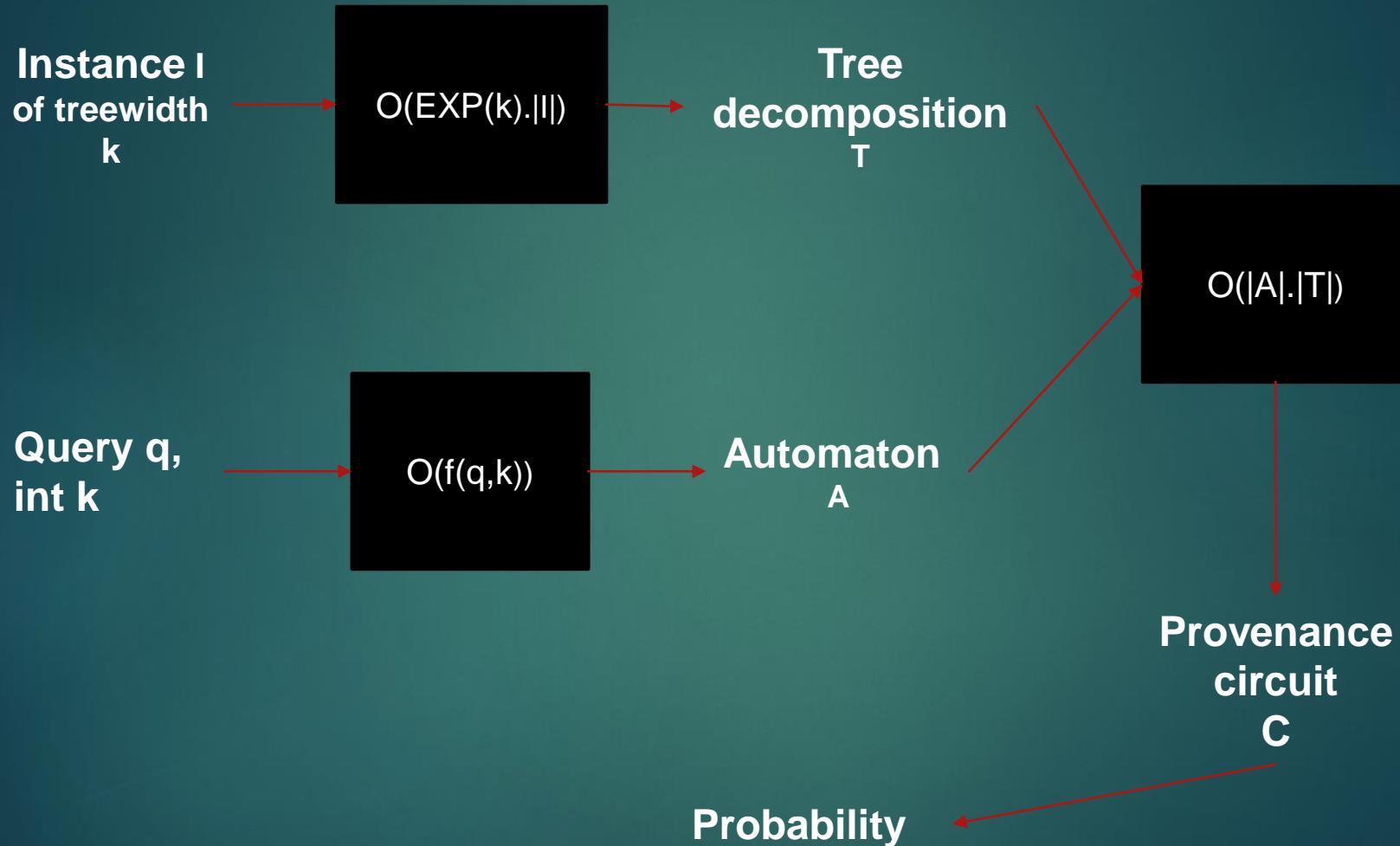
Query q,
int k

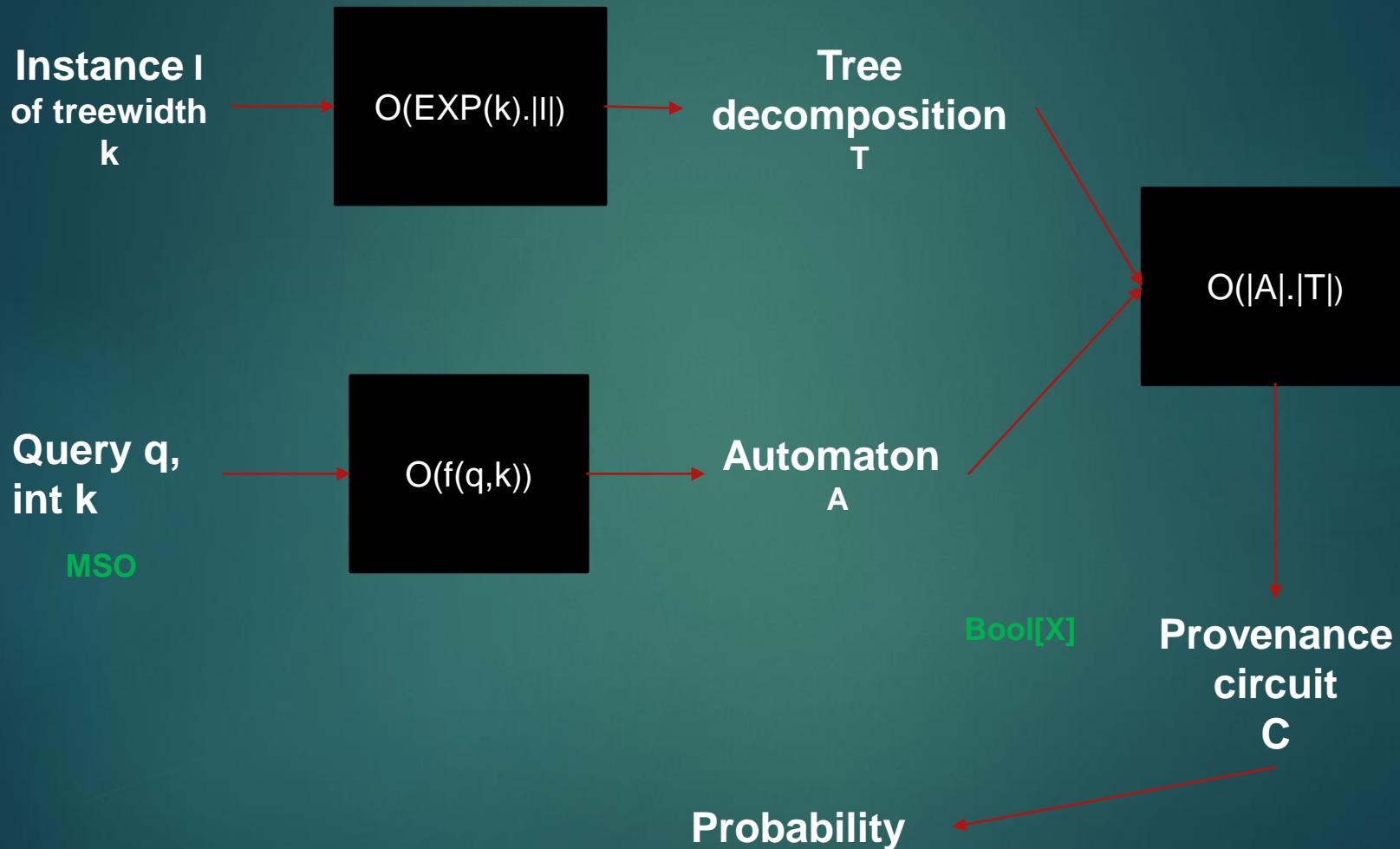
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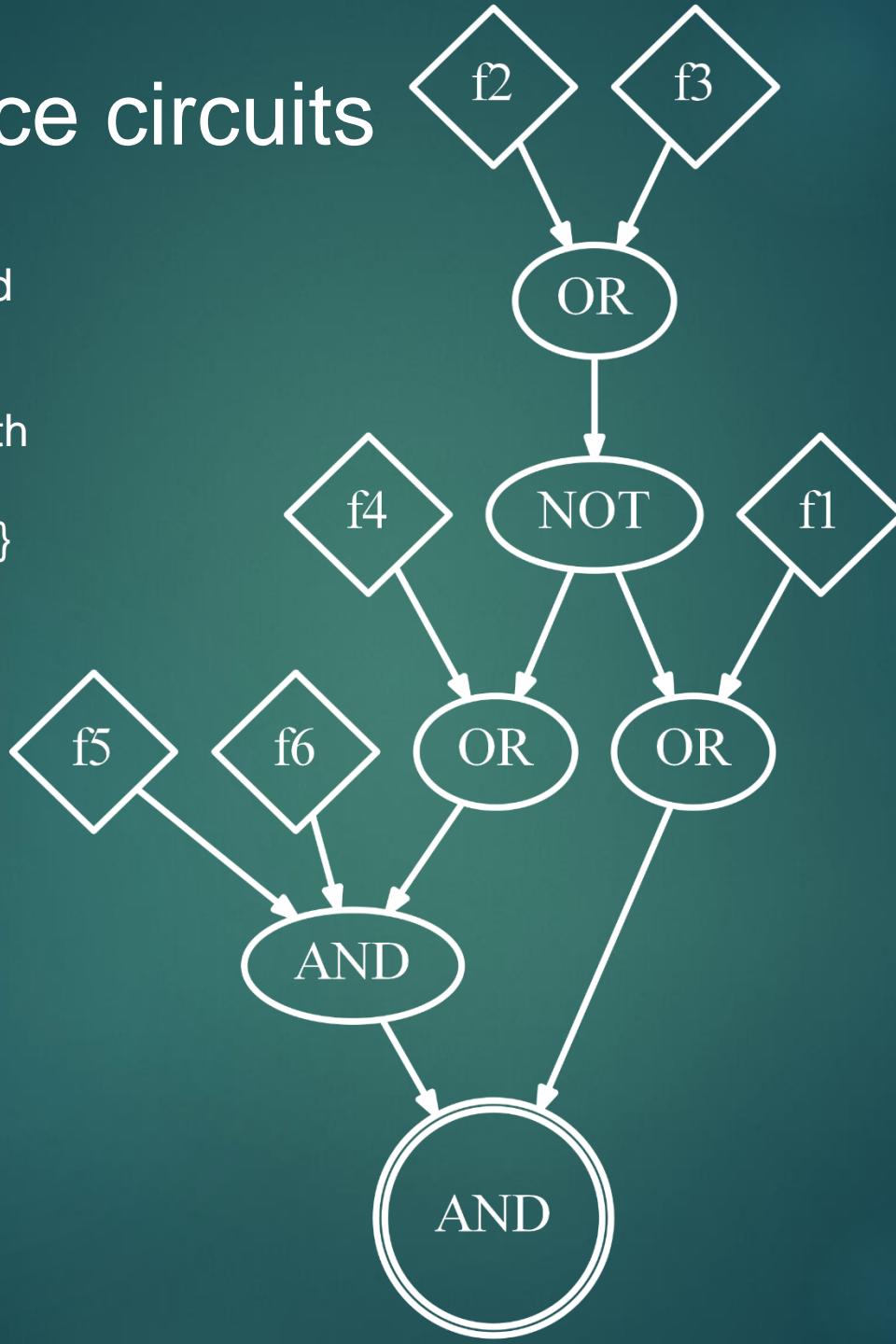




Provenance circuits

Some query q , fixed

Some instance I with
facts
 $\{f_1, f_2, f_3, f_4, f_5, f_6\}$

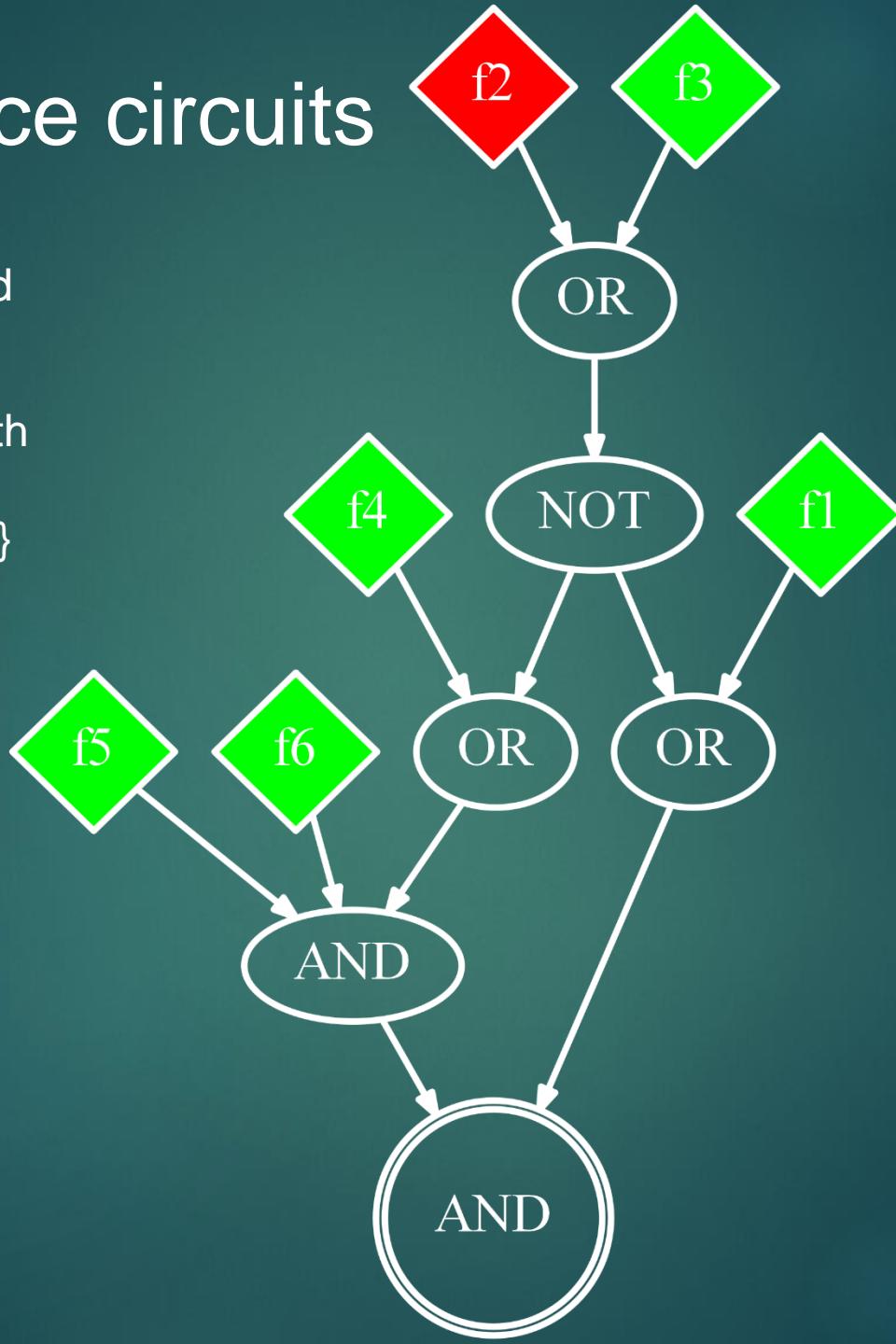


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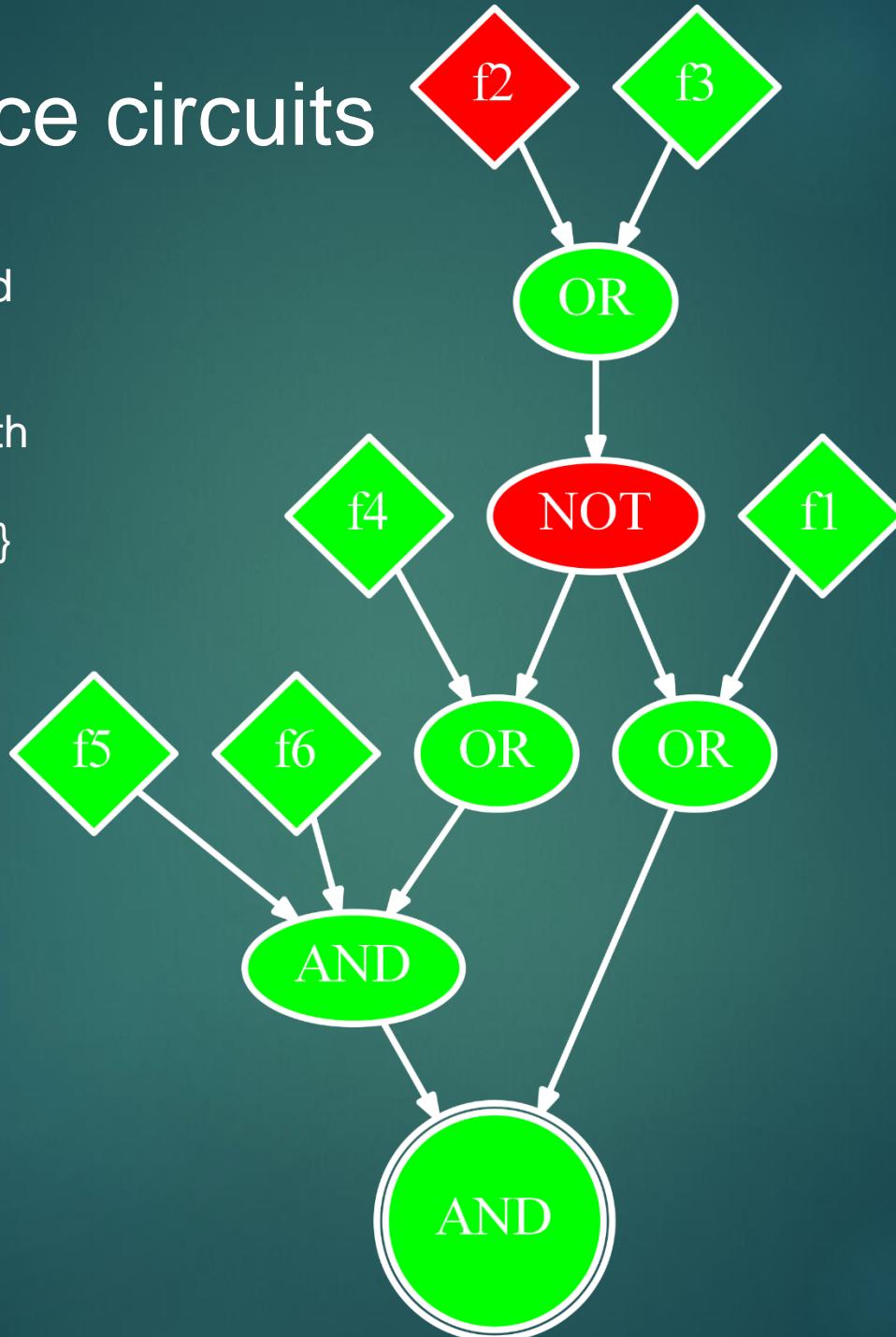


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Problems

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$$O(|A|.|T|)$$

Query q,
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Automaton
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Probability

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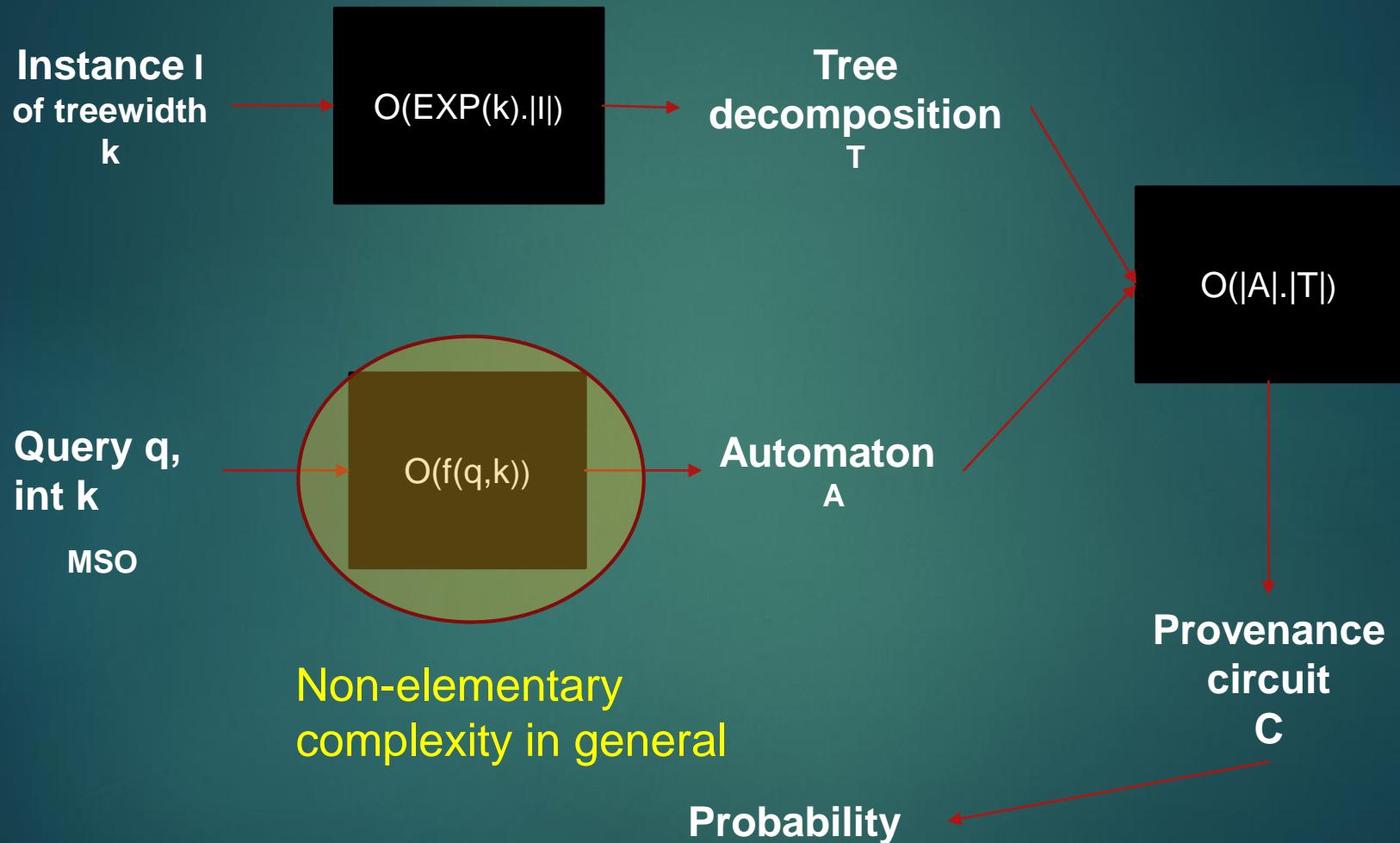
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$O(f(q,k))$

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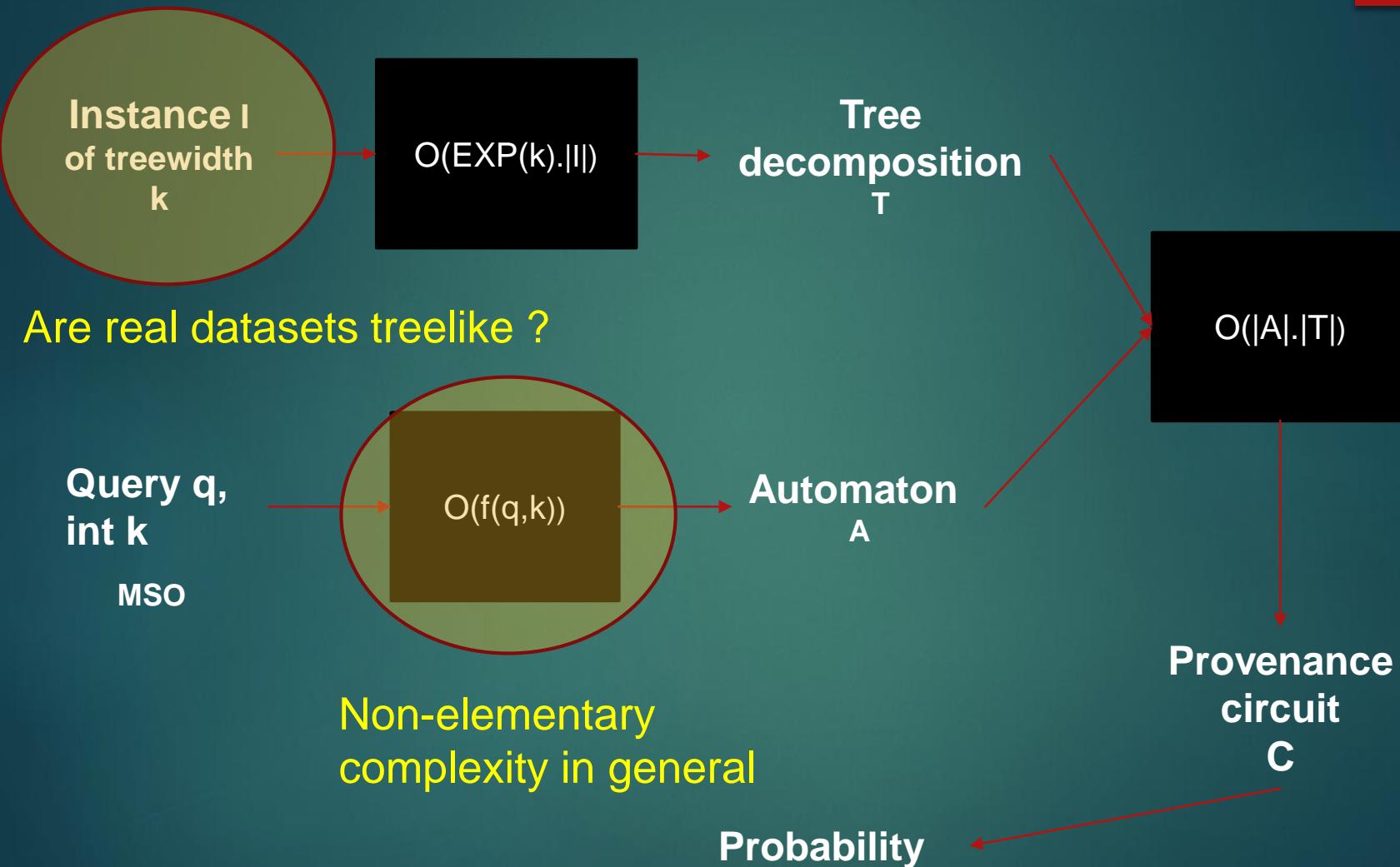
Provenance
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Non-elementary
complexity in general

Probability

Problems

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Current work

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Current work

- ▶ From bottom-up tree automata to alternating two-way automata

Current work

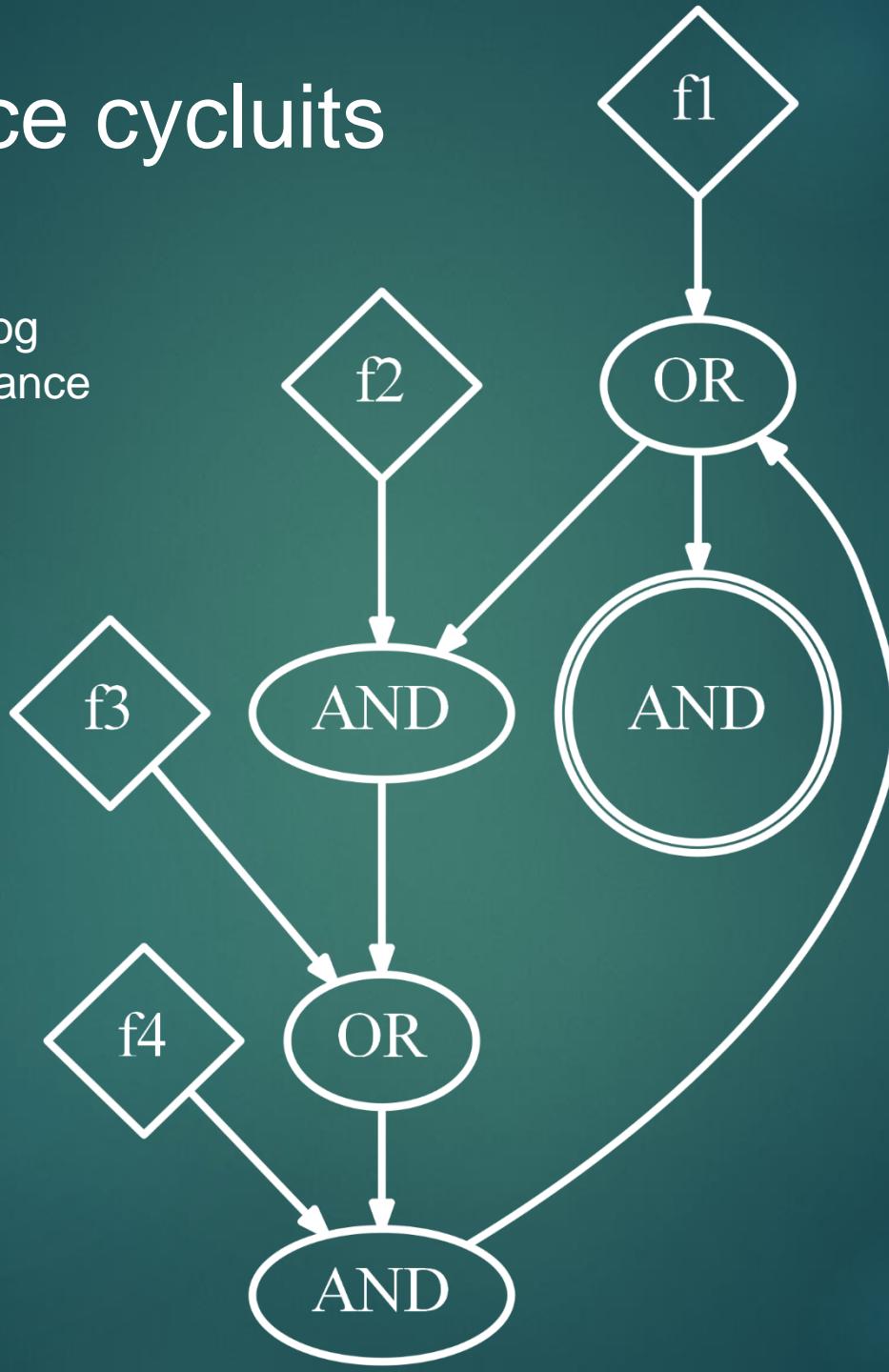
- ▶ From bottom-up tree automata to alternating two-way automata
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Current work

- ▶ From bottom-up tree automata to alternating two-way automata
- ▶ Introduce Intensionally-Clique-Guarded Datalog (ICG-Datalog) parameterized by body-size
- ▶ Provenance as a cyclic circuit ! (cycluit)

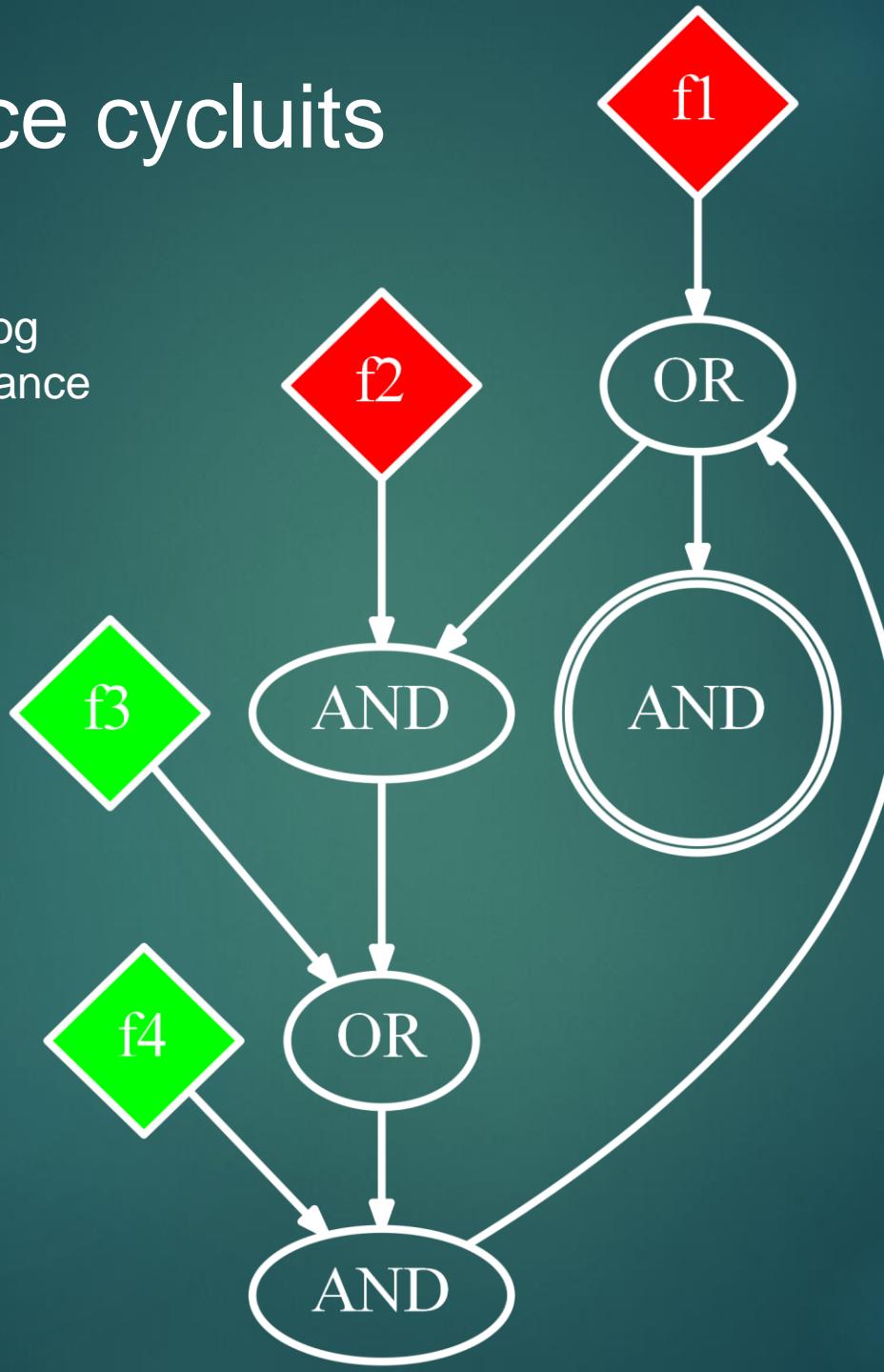
Provenance cycluits

Some ICG-Datalog
program, some instance
I with facts
 $\{f_1, f_2, f_3, f_4\}$



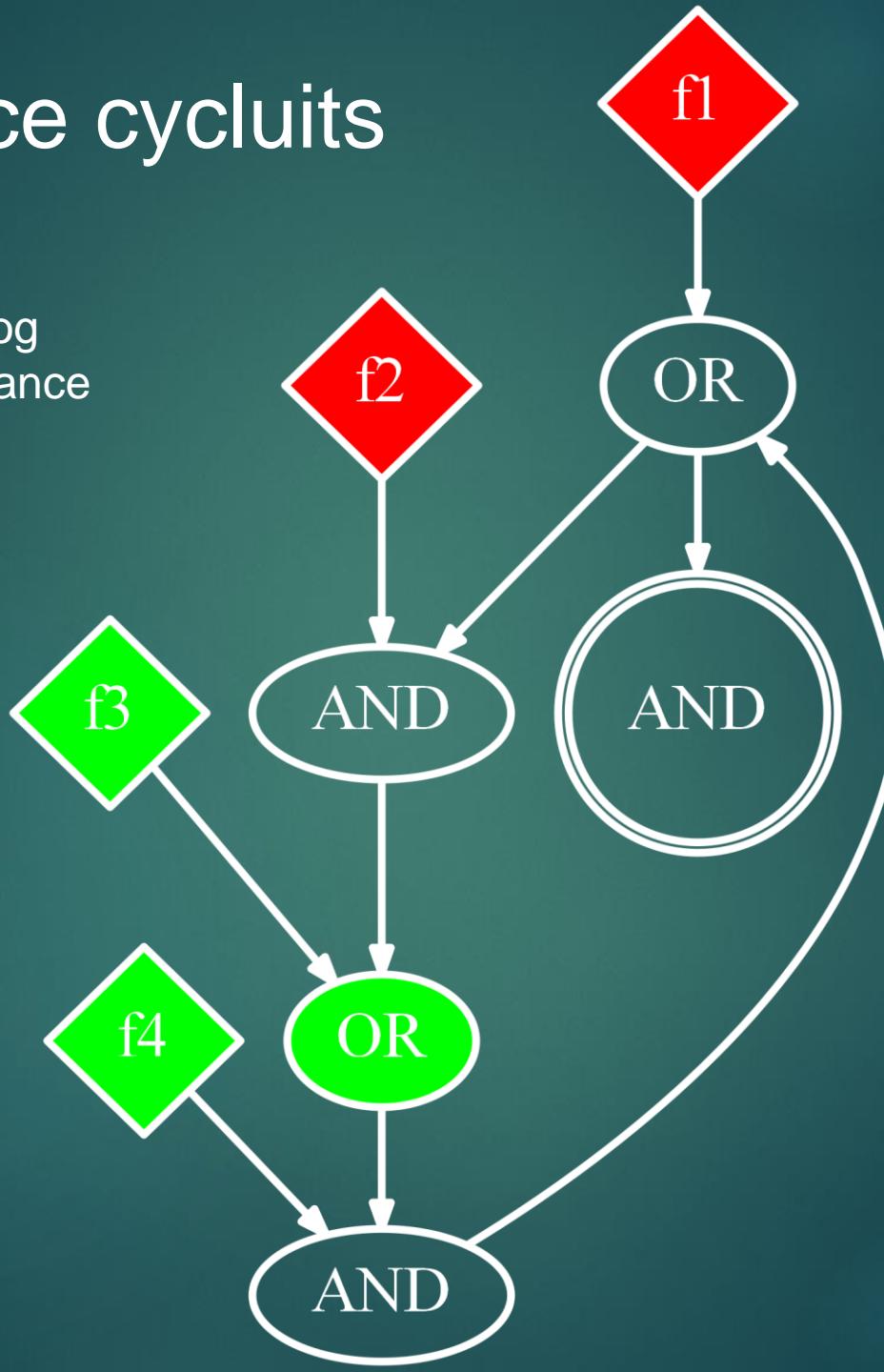
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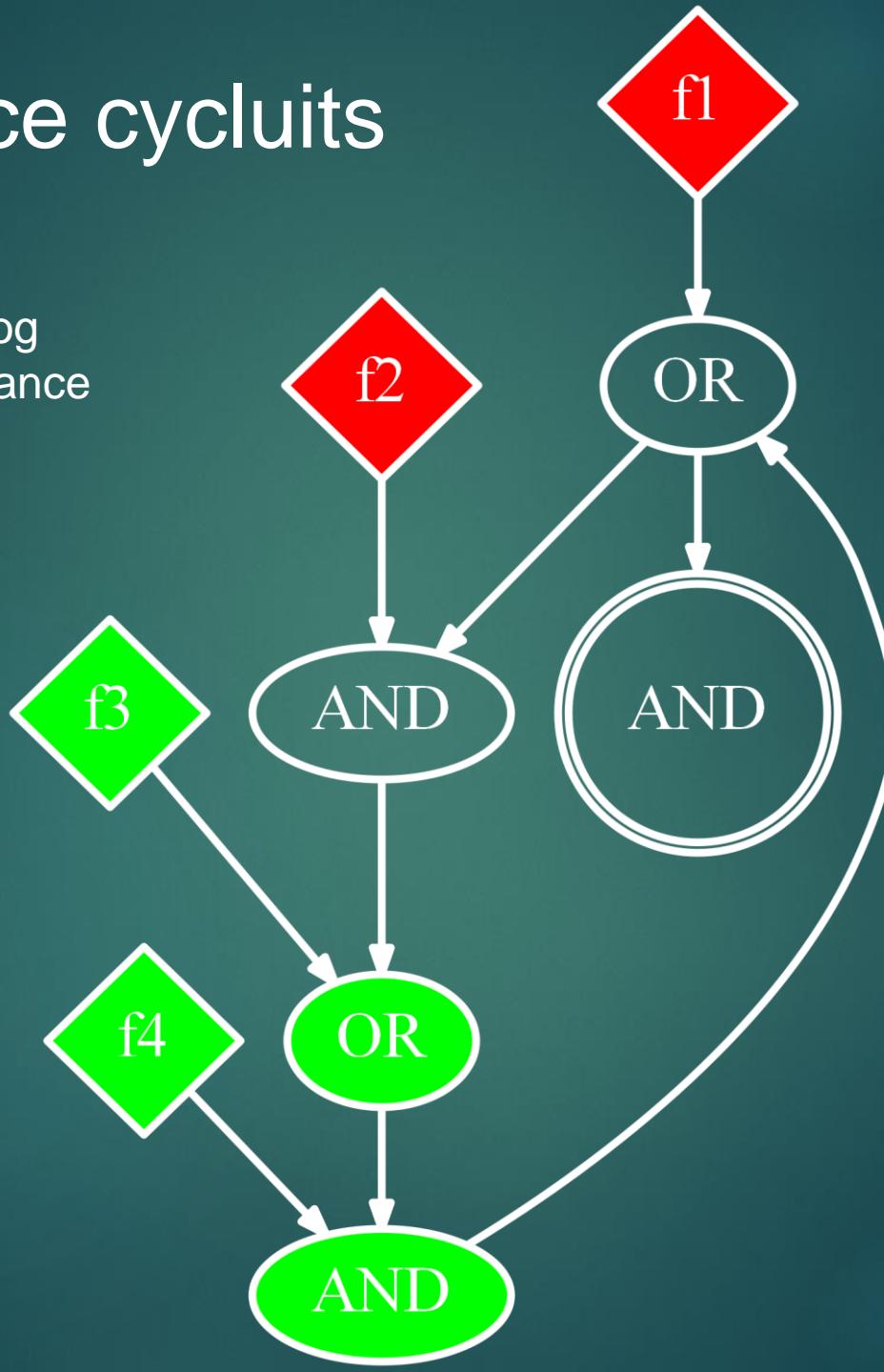
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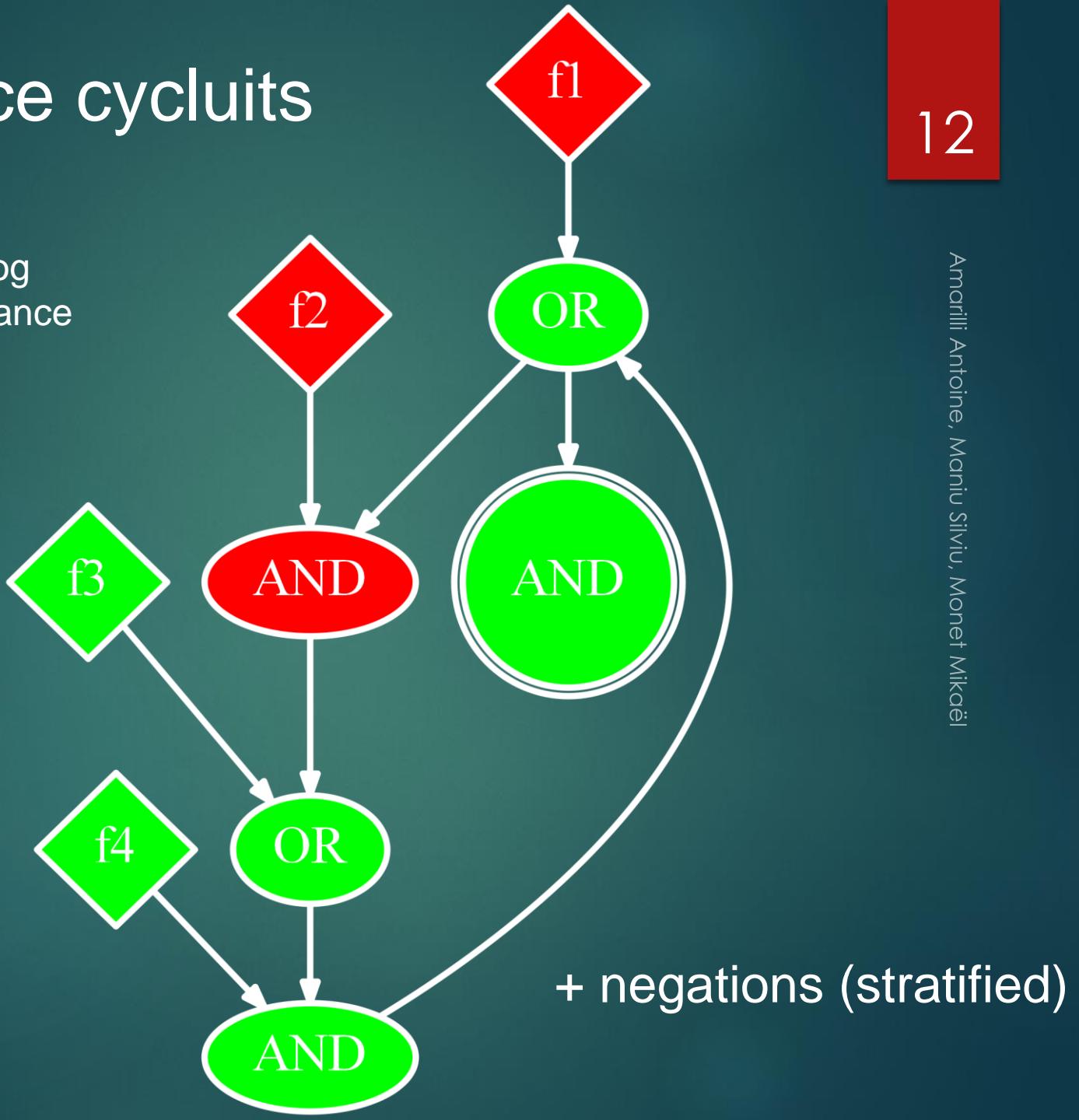
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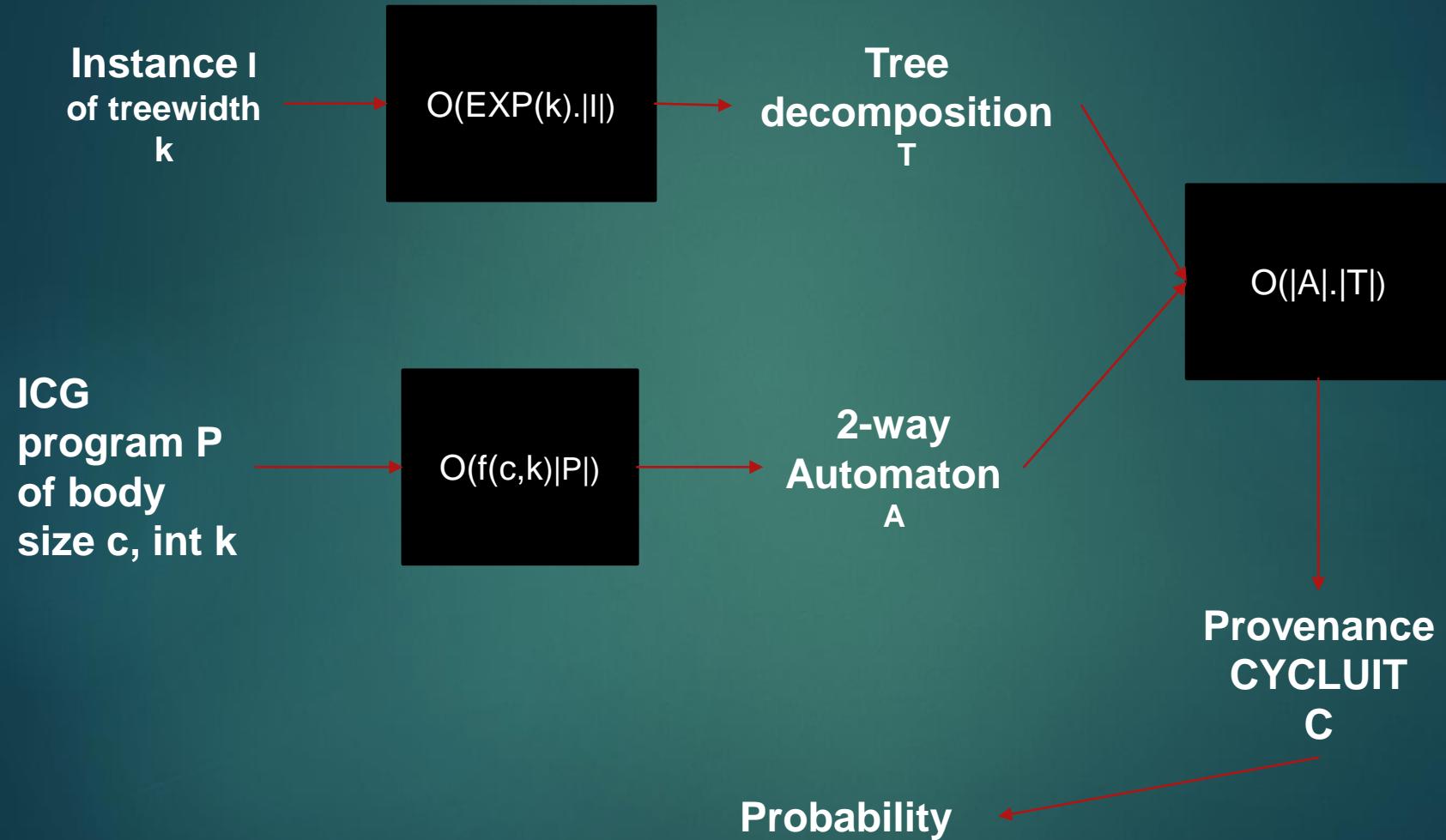
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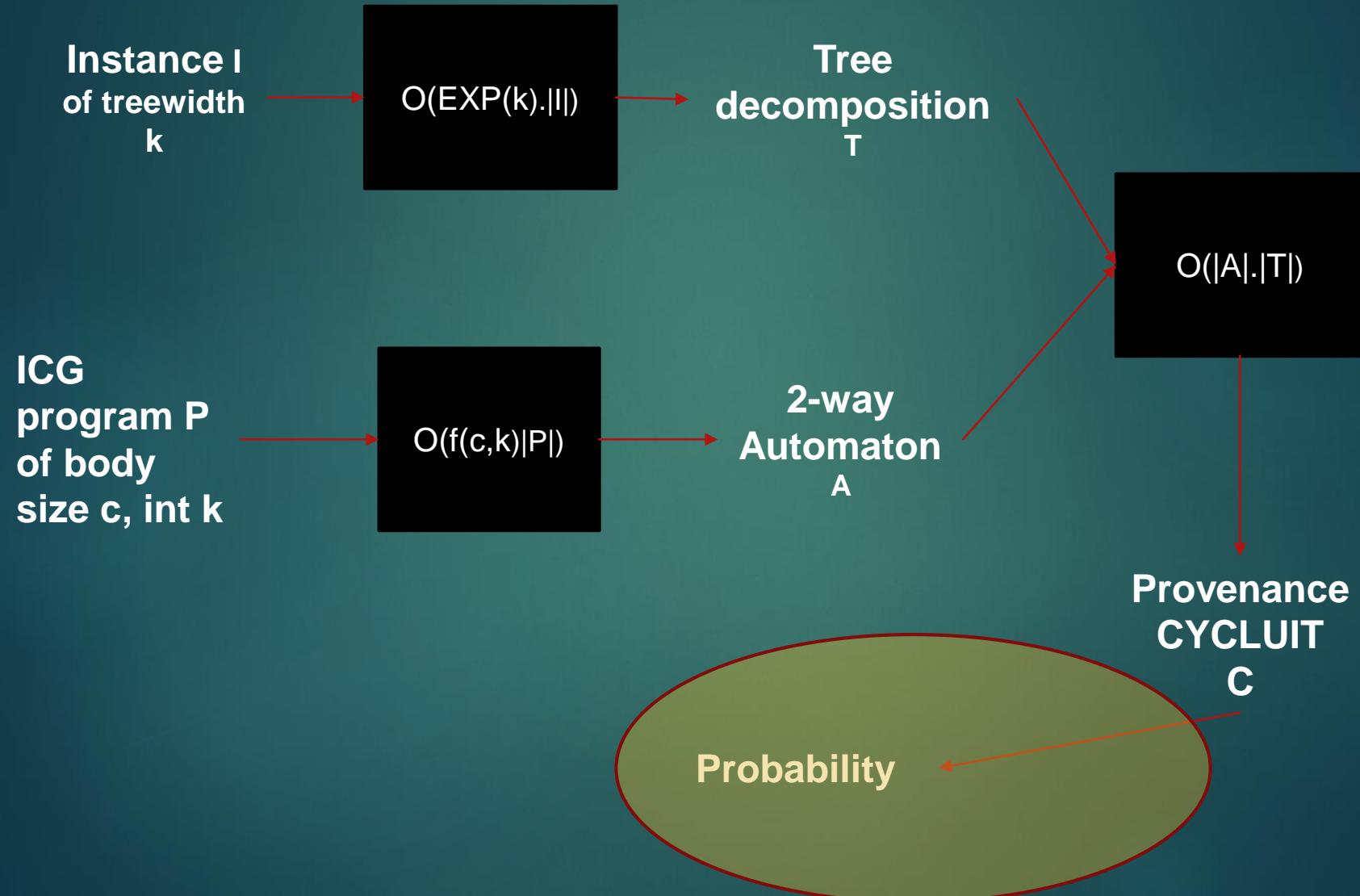


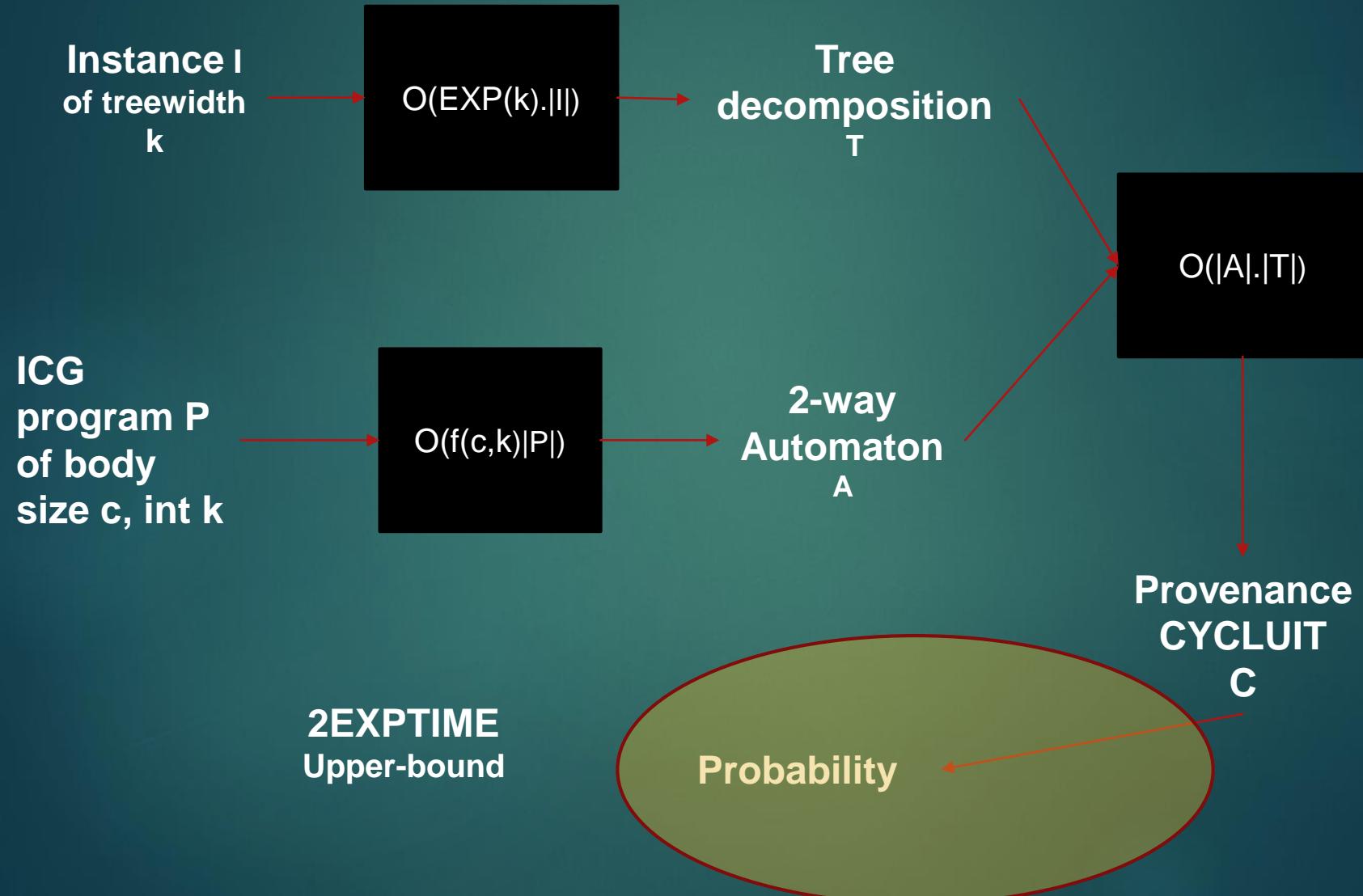
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Bad news...

- ▶ We proved that:

Path queries on tree instances (treewidth = 1) is already #P-hard. (reduction from #MONOTONE-2-SAT)

- ▶ Still, we obtain a 2EXPTIME combined complexity upperbound

Treelike datasets

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Treelike datasets

- ▶ Transportation networks

Treelike datasets

- ▶ Transportation networks
- ▶ Partial decompositions

Treelike datasets

- ▶ Transportation networks
- ▶ Partial decompositions
- ▶ Query-specific decompositions

